

if  $(n=1)$  { ... }  
 else { rec. }

$$T(n) = \begin{cases} 4T\left(\frac{n}{2}\right) + 3n, & n > 1 \\ 3 \text{ Base Case}, & n = 1 \end{cases}$$

$$T(n) = 4T\left(\frac{n}{2^1}\right) + 3n \quad | \text{ expand}$$

$$= 4\left(4T\left(\frac{n}{2^2}\right) + 3\frac{n}{2}\right) + 3n \quad | \text{ simplify}$$

$$= 4^2 T\left(\frac{n}{2^2}\right) + 4^1 \cdot 3\frac{n}{2} + 3n \quad | \text{ exp.}$$

$$= 4^3 \left(4T\left(\frac{n}{2^3}\right) + 3\frac{n}{2^2}\right) + 2^1 \cdot 3n + 3n \quad | \text{ simpl.}$$

$$= 4^3 T\left(\frac{n}{2^3}\right) + 3 \cdot 2^2 n + 3 \cdot 2^1 n + 3 \cdot 2^0 n \quad || \text{ TREND CLEAR}$$

$\log_2(n)$

$$\vdots \text{ down to } \frac{n}{2^{\log_2(n)}} + 3n \sum_{i=0}^{\log_2(n)-1} 2^i$$

$$= 4^{\log_2(n)} T\left(\frac{n}{2^{\log_2(n)}}\right) + 3n \left(2^{\log_2(n)} - 1\right)$$

$$= n^2 \cdot 3 + 3n(n-1)$$

$$= 3n^2 + 3n^2 - 3n$$

$$= 6n^2 - 3n \in \Theta(n^2)$$