Task

Given an integer $N\approx 10^6$ and a die that shows integers between 1 and 6 (inclusive) with equal probability. You repeat the following operation while your integer is strictly less than N:

• Roll the die. If it shows x, multiply your current integer by x.

Find the probability that your integer ends up being N. Come up with a fast algorithm.