

Extras 1

für sinusförmige Spannungen (z.B. $u(t) = \hat{u} \sin(t)$) gilt:

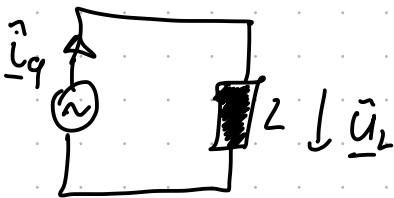
Effektivwert $U = \sqrt{\frac{1}{T} \int_0^T (\hat{u} \sin(t))^2 dt} = \sqrt{\frac{\hat{u}^2}{T} \int_0^T \sin^2(t) dt}$

$\sin^2(x) = \frac{1}{2}(1 - \cos(2x))$

$$= \sqrt{\frac{\hat{u}^2}{T} \int_0^T \frac{1}{2} - \frac{1}{2} \cos(2t) dt}$$
$$= \sqrt{\frac{\hat{u}^2}{T} \left(\frac{T}{2} - \frac{1}{2} \int_0^T \cos(2t) dt \right)}$$
$$= \sqrt{\frac{\hat{u}^2}{2T} \left(T - \underbrace{\left[\frac{\sin(2t)}{2} \right]_0^T}_0 \right)} = \sqrt{\frac{\hat{u}^2}{2}} = \frac{\hat{u}}{\sqrt{2}}$$

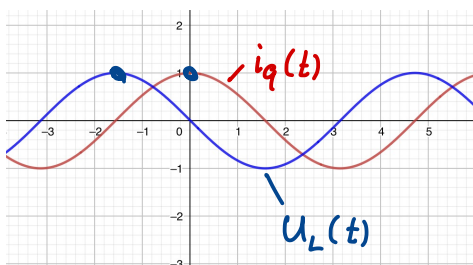
Frage:

gegeben: $i_q(t) = \hat{i} \cos(\omega t)$ ($\rightarrow \underline{\hat{i}}_q = \hat{i} e^{j0^\circ}$)

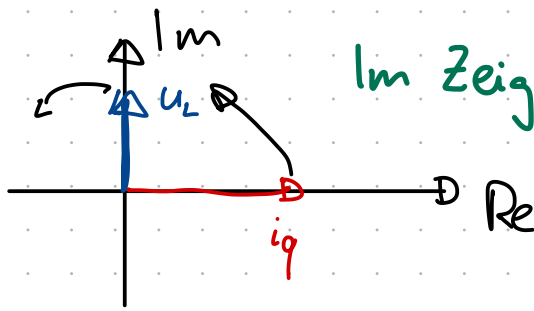


wie sieht $u_L(t)$ aus?

$$u_L(t) = L \frac{di_q(t)}{dt} = L \hat{i} \frac{d}{dt} \cos(\omega t) = L \hat{i} \omega \underbrace{(-\sin(\omega t))}_{\cos(\omega t + \frac{\pi}{2})}$$
$$= L \hat{i} \omega \cos(\omega t + \frac{\pi}{2})$$



$\hookrightarrow$ weiter links in Plot



Im Zeigerdiagramm sieht man, dass
der Strom nachhinkt