

Rekursion

```
void function(input size)
{
    base case → must be defined and reached!
    ... ..
    function(smaller input size) //recursive call
    ...*... ..
}

int main()
{
    ... ..
    function(input size)
    ... ..
}
```

- smaller subproblems must eventually reach the base case
- code must cover all smaller subproblems
- base case cannot have recursive calls i.e. defined in a non-recursive manner.
- recursive call should call with smaller input size and should make progress toward base case
- in each call: think how you can use the solution of smaller subproblems to solve the current input size
- you can have several different calls here dep on some condition/constraint on the input e.g. n odd → n even →

code examples : power function

```
3 // POST: result == x^n
4 unsigned int power(const unsigned int x, const unsigned int n)
5 {
6     if (n == 0)
7     {
8         return 1;
9     }
10    else if (n == 1)
11    {
12        return x;
13    }
14    else if (n % 2 == 0)
15    {
16        int temp = power(x, n / 2);
17        return temp * temp;
18    }
19    else
20    {
21        return x * power(x, n - 1);
22    }
23 }
```

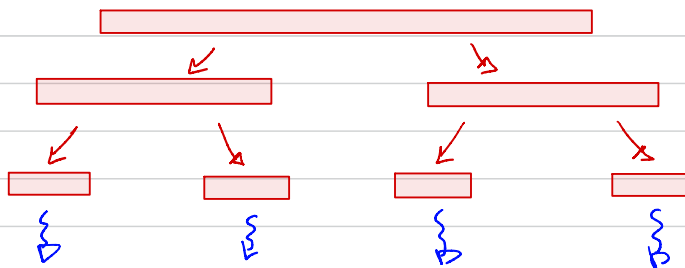
two non-recursive calls

two recursive calls

→ this shows nicely, that it is possible and sometimes smart to differentiate between several base cases and several recursive calls.

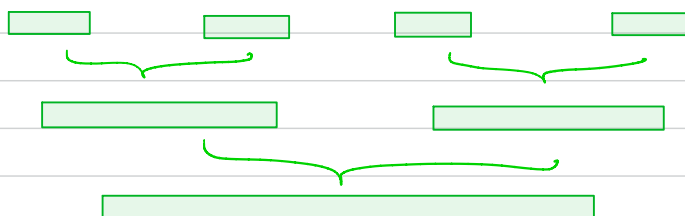
"Divide and Conquer"

e.g. problem of size n



divide problem into smaller subproblems

conquer the smaller subproblems $\hat{=}$ solve problem for small size



combine the results from the smaller problems to get final result

```
#include<iostream>
```

```
unsigned int partial_sum(const unsigned int n) {  
    if (n == 0)  
        return 0;  
    else {  
        // print descending  
        // std::cout << n << std::endl;  
        unsigned int partial = partial_sum(n - 1);  
        // print ascending  
        std::cout << n << std::endl;  
        return n + partial;  
    }  
}
```

```
int main() {  
    std::cout << "n = ";  
    unsigned int n;  
    std::cin >> n;  
    std::cout << partial_sum(n) << std::endl;  
    return 0;  
}
```

PS(5)

